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# RFC 5170 / LDPC-\* codes: recommendations for their optimal use

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## Summary

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- recent results have shown LDPC-staircase /triangle codes are:

- **very close** to ideal codes
- one order of magnitude **faster** than Reed-Solomon over  $GF(2^8)$  (using Rizzo's reference codec)

...in **many** use-cases


- made possible by
  - hybrid Zyablov Iterative decoding/Gaussian elimination scheme, and...
  - the new N1 parameter

## Summary... (cont')

### ● N1 parameter

- number of “1s” in each column of the parity check matrix during the first step of the algorithm

add N1 “1s”


$$[H_1 | Id_3] = \left( \begin{array}{ccc|ccc} s_1 & \dots & s_6 & p_7 & p_8 & p_9 \\ \hline 0 & 1 & 0 & 1 & 1 & 1 \\ 1 & 1 & 1 & 0 & 0 & 1 \\ 1 & 0 & 1 & 1 & 1 & 0 \end{array} \right) \begin{matrix} c_1 \\ c_2 \\ c_3 \end{matrix}$$

- N1 was fixed and equal to 3 until 08 version, but **now**:
  - N1 belongs to {3; 10} (N1=3 remains the default)
  - N1 is set by the encoder...
  - ...and communicated to the decoder (in EXT\_FTI or FDT)
  - increases the density of the matrix... and the probability it is invertible!

## LDPC performances

### ● depend on:

- decoding scheme used
- N1 parameter with LDPC-staircase codes (≠ triangle)

### ● more specifically

- the decoder has to solve a **system of linear equations**
- possible with Zyablov Iterative Decoding (ID) scheme
  - fast but sub-optimal erasure recovery
- or **Gaussian elimination (GE)**
  - optimal erasure recovery but more costly
- or **intelligent variants of ID**
  - see Raptor/RFC 5053 and associated [US patent 6,856,263](#)

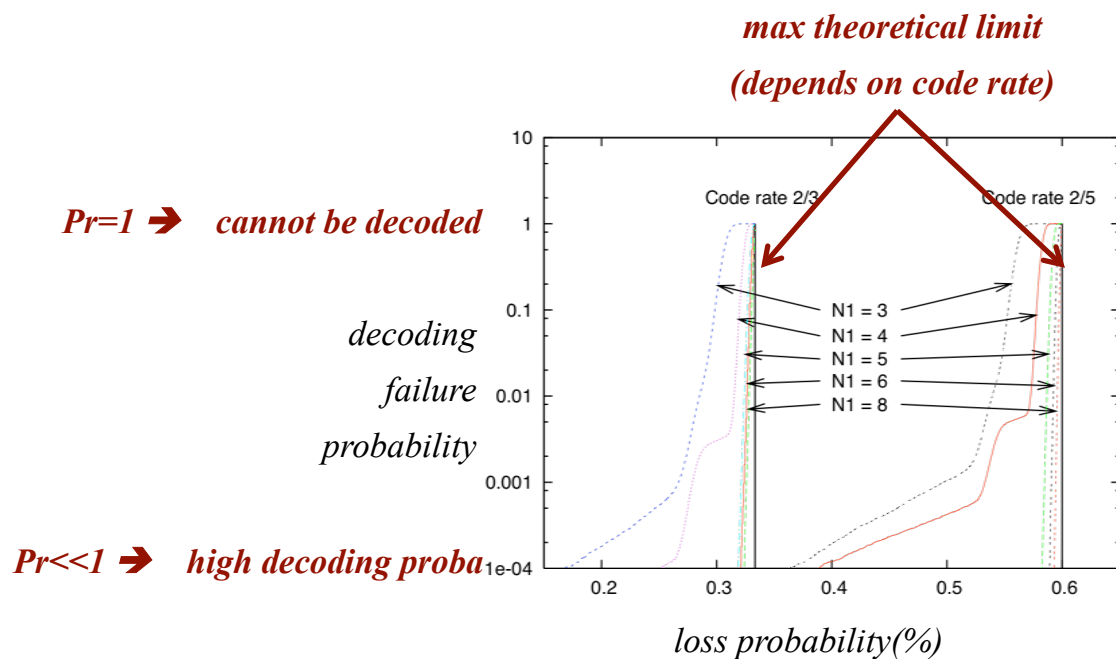
## LDPC performances... (cont')

- ...or with a **hybrid ID/GE** scheme

- **recommended** for small to medium sized objects
- **start decoding with ID**
  - it's perhaps sufficient...
  - if not, it will anyway simplify the system
- **finish with GE (e.g., if it's known that no additional symbols will be received)**
  - works on the system simplified by the ID, not the original one!

## Erasure recovery results

- example: LDPC-staircase, various N1 values



## Erasure recovery results... (cont')

### ● LDPC-staircase results (N1=5, k=1,000)

code rate	average overhead	overhead for a failure proba $\leq 10^{-4}$
2/3 (=0.66)	0.63%	2.21%
2/5 (=0.4) (worst case!)	2.04%	4.41%

- then results further improve as the code rate decreases
  - not shown here, see [SPSC08]
  - means that **small-rate codes are feasible...**
- results remain excellent with smaller objects
  - no need to artificially increase the number of symbols...
    - symbols groups are no longer needed → use G=1 (default)
  - this is the opposite with ID!

## Decoding complexity results

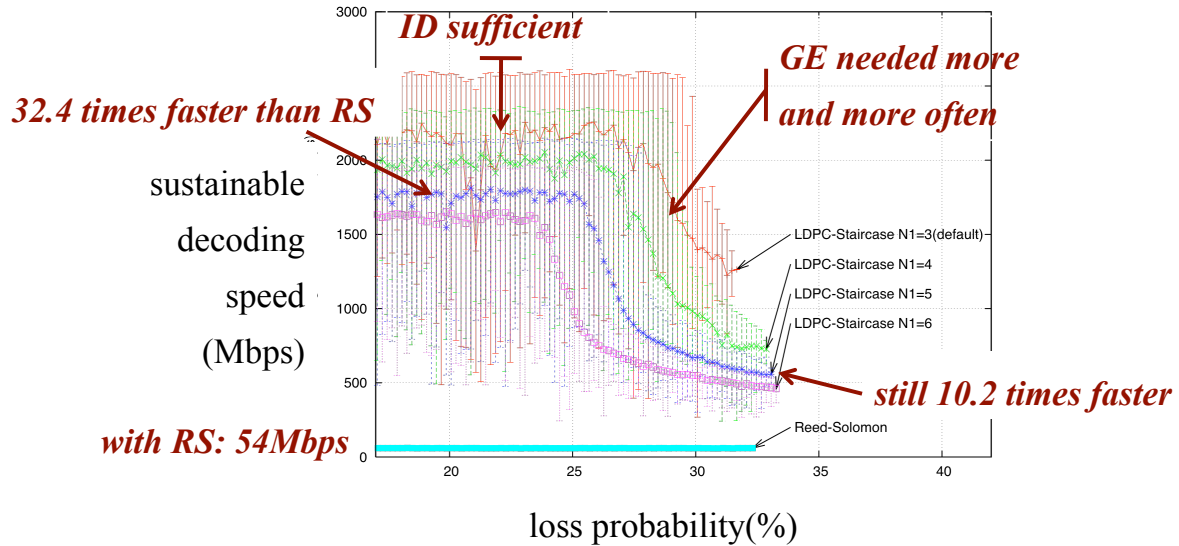
### ● complexity depends on:

- block size (GE complexity increases)
- loss rate (is ID sufficient or should GE be used too?)
- N1 parameter with LDPC-staircase codes (the linear system complexity increases with N1)

## Decoding complexity results... (cont')

- example: LDPC-staircase, code rate 2/3, k=1,000

- the higher N1, the more complex the decoding
- yet with N1=5, between **32 to 10 times faster than RS(2<sup>8</sup>)**



## Decoding complexity results... (cont')

- we see that:

- decoding complexity **isn't prohibitive at all** with objects that are a few thousands of symbols long 😊
- it requires a careful implementation though
  - take into account the specific parity check matrix structure
- these results are not the ultimate ones and we should be able to further reduce the decoding complexity...



## To conclude

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- with small/medium sized objects
  - prefer hybrid decoding
  - use  $G=1$  (no symbol grouping), it's useless now
  - with larger objects, fall back to ID
- optimal LDPC-triangle codes performances
  - achieved with  $N1=3$  (default) for ID or hybrid decoding
- optimal LDPC-staircase codes performances
  - require an appropriate  $N1$  value
    - $N1=3$  (default) is the best for ID
    - $N1=4$  or  $5$  is recommended with hybrid decoding



## References

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*General idea  
triangle  
results...*

- “Improving the Decoding of LDPC Codes for the Packet Erasure Channel with a Hybrid Zyablov Iterative Decoding/Gaussian Elimination Scheme”,  
INRIA Research Report RR-6473, March 2008  
<http://hal.inria.fr/inria-00263682/en/>

*Additional  
results for  
staircase  
codes...*

- “Optimizing the Error Recovery Capabilities of LDPC -staircase Codes Featuring a Gaussian Elimination Decoding Scheme”,  
June 2008, to appear in SPSC'08.  
<http://hal.inria.fr/inria-00291656/en/>